

ZESTAW I

Zad. 2

Rozwiąż równanie:

d)

$$\operatorname{tg}(2\operatorname{arctg}3x) = \sqrt{3}$$

$$\text{niech : } t = 2\operatorname{arctg}3x \quad \mathbb{Z} : t \in (-\pi; \pi)$$

$$\operatorname{tgt} = \sqrt{3}$$

$$t = -\frac{2}{3}\pi \vee t = \frac{\pi}{3}$$

stąd :

$$2\operatorname{arctg}3x = -\frac{2}{3}\pi \vee 2\operatorname{arctg}3x = \frac{\pi}{3}$$

$$\operatorname{arctg}3x = -\frac{\pi}{3} \vee \operatorname{arctg}3x = \frac{\pi}{6}$$

$$3x = -\sqrt{3} \vee 3x = \frac{\sqrt{3}}{3}$$

$$x = -\frac{\sqrt{3}}{3} \vee x = \frac{\sqrt{3}}{9}$$

$$\text{Odp : } x \in \left\{-\frac{\sqrt{3}}{3}; \frac{\sqrt{3}}{9}\right\}$$

e)

$$\operatorname{tg}\left(\frac{1}{2}\operatorname{arctg}x\right) = \sqrt{3}$$

$$\text{niech : } t = \frac{1}{2}\operatorname{arctg}x \quad \mathbb{Z} : t \in \left(-\frac{\pi}{4}; \frac{\pi}{4}\right)$$

$$\operatorname{tgt} = \sqrt{3}$$

$$t \in \emptyset$$

Powyższe równanie nie ma rozwiązań

$$\text{Odp : } x \in \emptyset.$$